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# K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub>: A transparent nonlinear optical crystal with frustrated magnetism

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### 1. Introduction

The large family of borate compounds, acting as a "chemical playground" of structure design for functional materials, has provided an expansive area of research for over 50 years owing to the extremely wide variability of borate crystal chemistry and their good chemical stability [1-3]. Since the advent of low-temperature BaB<sub>2</sub>O<sub>4</sub> (BBO) and LiB<sub>3</sub>O<sub>5</sub> (LBO) as two efficient nonlinear optical (NLO) materials [4,5], various main-group metal borates have been discovered and suggested for NLO applications, especially in UV region because of their high UV transmittance and high damage threshold. Besides, transition-metal borates and rare-earth-metal borates integrating in one crystalline matrix with two or more physical features are also the focus of both theoretical and experimental studies. The presence of *d*- or *f*-block elements in these borates results in a variety of technologically important properties, and they emerge as important multifunctional materials when given optical characteristics are combined with magnetic or electric properties. Metal borates of the general formula  $RM_3(BO_3)_4$  (R=Y, La–Lu; M=AI, Ga, Fe, Cr, Sc) [6–10], crystallizing in the trigonal structure of the mineral huntite CaMg<sub>3</sub>(CO<sub>3</sub>)<sub>4</sub> type (space group R32), are the most widely developed system. They are classed as new-generation materials for lasers in respect that they exhibit both luminescence and secondharmonic generation (SHG) properties. Nd-doped YAl<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> and GdAl<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub> crystals as the two representatives of this family have been widely studied and applied in self-frequency-doubling laser

## ABSTRACT

A new noncentrosymmetric ferroborate crystal,  $K_2Fe_2B_2O_7$ , has been grown from high temperature melt. Structure solution from single crystal X-ray diffraction shows that the title compound crystallizes in a trigonal space group P321 with cell dimensions of a=8.7475(12)Å and c=8.5124(17)Å. In the structure, FeO<sub>4</sub> tetrahedron shares its three basal oxygen atoms with BO<sub>3</sub> triangles forming a twodimensional layer in the *ab* plane and the layers are connected by the apical Fe–O bonds along the *c* direction. The crystal is transparent in the visible and near infrared region from 500 to 2000 nm with three pronounced absorption bands ascribed to d-d transitions of tetrahedrally coordinated Fe<sup>3+</sup> ions. Though, structurally analog to K<sub>2</sub>Al<sub>2</sub>B<sub>2</sub>O<sub>7</sub>, the further twisting of the BO<sub>3</sub> groups between adjacent layers reduces its optical nonlinearity to a second-harmonic generation intensity of about 0.4 times that of KDP. Spin-glass behavior is observed at 20 K which is probably due to geometrically magnetic frustration of the triangular Fe net in the *ab* plane.

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sources [11–14]. Another interesting aspect of  $RM_3(BO_3)_4$  system is that when *M* is a transition metal element (like Fe or Cr), the well separated  $MO_6$  helical magnetic chains interact mutually and also interact with the magnetic rare earth ions leading to complicated magnetic behaviors which endue them with promising magneto-optical and other multi-ferroic properties [15–17].

There are only a few borates containing trivalent iron ion (socalled ferroborate) showing magnetic ordering: FeBO<sub>3</sub> [18], Fe<sub>3</sub>BO<sub>6</sub> [19],  $RFe_3(BO_3)_4$  (R=Y, La–Lu) [20], and  $Fe(M^{II}O)_n(BO_3)$  (M=Co, Mn,Zn, n=1; M=Cu, Ni, n=2) [21]. As a well-known weak ferromagnet, iron borate FeBO<sub>3</sub> represents a rare example of a magnetically ordered ferric oxide with high transparency in the visible spectral region and important magneto-optical properties [18d,18e]. When we concentrated on the study of d-d transitions in Fe-doped K<sub>2</sub>Al<sub>2</sub>B<sub>2</sub>O<sub>7</sub> (KABO) crystals [22], we found that as the content of iron increases, Xray diffraction peaks shift towards lower  $2\theta$  values from pure KABO gradually, which indicates the formation of  $K_2(Fe_xAl_{1-x})_2B_2O_7$  solid solution, whereas the crystal system maintains. At the end, a new compound K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub>, structurally analog to KABO with the aluminum fully substituted by iron, was obtained. K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> crystal shows high transparency in the visible and IR region, considerable SHG efficiency and interesting magnetic properties.

## 2. Experiment section

## 2.1. Crystal growth and X-ray diffraction

Single crystals of  $K_2Fe_2B_2O_7$  were grown by spontaneous nucleation in a platinum crucible from the melt of analytical

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reagent (AR) grade K<sub>2</sub>CO<sub>3</sub>, Fe<sub>2</sub>O<sub>3</sub> and H<sub>3</sub>BO<sub>3</sub> in molar ratios of K:Fe:B=1:1:1.2. The melt was cooled from 900 to 800 °C at a rate of 2 °C/h and then to room temperature with power off. Platelet crystals appeared at the surface in the crucible and they were mechanically separated from the solution surface. Typical products consist transparent, yellowish crystal sheets with size up to  $2.5 \times 2.5 \times 0.2 \text{ mm}^3$  (see Appendices, Fig. A1).

The structure of K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> was determined by single-crystal X-ray diffraction on a Rigaku AFC10 diffractometer equipped with MoK $\alpha$  radiation ( $\lambda$ =0.71073 Å). Data were collected at low temperature (93 K) with  $\theta$  range from 3.60° to 27.47°. A total of 4534 reflections were measured, of which 874 unique ones were used for the structure solution. The crystal structure was solved and refined by SHELXS-97 and SHELXL-97 packages [23], adopting the structural parameters of KABO as an initial structure model. Final agreement indices of *w*R2=0.0540 and R1=0.0282 were obtained. The final difference electron-density map shows a highest peak of 0.50 eÅ<sup>-3</sup> located 0.78 Å from O1 and a deepest hole of -0.67 eÅ<sup>-3</sup> located 0.32 Å from Fe1. Further crystallographic parameters and the refined structural data are provided in Table 1.

# 2.2. Physical property measurements

Optical transmittance spectrum was recorded with a Lambda 900 UV–VIS–NIR (Perkin-Elmer) spectrophotometer in the region of 185–2000 nm and the thermal stability of the title compound was analyzed with differential thermal analysis (DTA) under static air in a WCR-2A DTA instrument. For the powder SHG intensity measurement, a Nd<sup>3+</sup>:YAG laser of wavelength 1064 nm was used as incident light and the frequency-doubled outputs were recorded using KDP as a reference. Since the powder SHG efficiency depends strongly on particle size based on the Kurtz–Perry method [24], the K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> crystals were ground and sieved into distinct particle sizes varying from 20 to 150  $\mu$ m.

Temperature dependence of the *dc* magnetic susceptibility was measured on a superconducting quantum interference device magnetometer (SQUID, Quantum Design) under field cooled (FC) and zero field cooled (ZFC) conditions. Data were collected over the temperature range 5–400 K with an applied field of 1000 G.

#### 3. Results and discussion

#### 3.1. Structure

 $K_2Fe_2B_2O_7$  crystallizes in the trigonal space group *P*321 with lattice parameters a=b=8.7475(12)Å and c=8.5124(17)Å and

Table 1	
Refined structural data of K <sub>2</sub> Fe <sub>2</sub> B <sub>2</sub> O <sub>7</sub> at 93 K	

Atom	x	у	Z	$U_{\rm eq}$ (Å <sup>2</sup> )
Fe1	0	0	0.71048(8)	0.0045(2)
Fe2	2/3	1/3	0.80960(8)	0.0049(2)
Fe3	1/3	2/3	0.76756(8)	0.0051(2)
K1	0.68190(11)	0	0	0.0097(2)
K2	0.64708(11)	0	0.5	0.0097(2)
01	0	0	0.5	0.0132(11)
02	1/3	2/3	0.9789(4)	0.0165(9)
03	0.5630(3)	0.7391(3)	0.6991(3)	0.0103(5)
04	0.8978(3)	0.4124(3)	0.7429(3)	0.0109(5)
05	0.2283(3)	0.0669(3)	0.7810(3)	0.0101(5)
В	0.0010(4)	0.3358(5)	0.7411(4)	0.0069(8)

Space group: P321 a=b=8.7475(12)Å and c=8.5124(17)Å. R1=0.0282 and wR2=0.0540 for all data.

exhibits a layered structure composed by the arrangement of BO<sub>3</sub> triangles and tetrahedral FeO<sub>4</sub> groups (shown in Fig. 1). There are three crystallographically independent Fe sites leading to three different types of distorted FeO<sub>4</sub> units and forming two types of apical sharing tetrahedral FeO<sub>4</sub> pairs with 180° Fe1-O1-Fe1 and Fe<sub>2</sub>-O<sub>2</sub>-Fe<sub>3</sub> bonds. It is found that the three tetrahedral FeO<sub>4</sub> units are almost identical with little variations of the basal Fe-O bonds ranging from 1.868(2) to 1.877(2)Å and the apical Fe–O bonds varying from 1.7917(8) to 1.800(3)Å. The observation of significant shortening of the apical bonds can also be found in KABO [25], where the distances of the basal and apical Al–O bonds are observed as 1.756 and 1.700 Å, respectively. The bottom surfaces of all the FeO<sub>4</sub> tetrahedra share corners with three adjacent BO<sub>3</sub> triangles to form six-membered rings, which produce a triangular Fe lattice parallel to the *ab* crystal plane. These two groups formed a nearly planar [Fe<sub>3</sub>B<sub>3</sub>O<sub>6</sub>] framework with all the planes of BO<sub>3</sub> groups approximately perpendicular to the *c* axis. The average bond length for B–O is 1.374 Å and the mean O–B–O bond angle is close to 120°, which are in accordance with the ideal BO3 triangle having a B-O distance and O-B-O angle of 1.368 Å and 120° [26]. The selected inter-atomic distances and bond angles of K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> are shown in Table 2.

K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> is structurally closely related to KABO, both of which contain planar [BO<sub>3</sub>]<sup>3-</sup> groups as their major NLO active units [25b,25c]. The contrasting BO<sub>3</sub> groups' arrangements in the unit cells of K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> and KABO are shown in Fig. 2. It is found that in K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> structure, BO<sub>3</sub> groups are twisted about 50° from those of adjacent layers, whereas the angle of twist is only 40° in KABO. The further twisting of BO3 triangles in K2Fe2B2O7 may be attributed to the longer in-plane Fe-O bonds than that of the Al-O bonds. In order to host the much longer Fe-O bonds in a K-O set lattice, the BO<sub>3</sub> triangles are forced to twist, giving a much bent Fe–O–B bonds. According to the anionic group model for borate compounds proposed by Chen et al. [27], the BO<sub>3</sub> groups are considered to be the most basic structural units responsible for optical nonlinearity, and the bulk NLO properties can be calculated by summating their respective contributions. Consequently, the SHG coefficient of K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> can be calculated as  $d_{11} = -0.315 \text{ pm}/$ V, which is smaller than that of KABO (calculated:  $d_{11} = 0.585 \text{ pm/V}$ , experimental:  $d_{11}=0.46 \text{ pm/V}$  [28,29]. Fig. 3 shows the experimental SHG signal intensities of K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> powder with different particle sizes relative to KDP standard and it gives a maximum value of about 0.4 times that of KDP despite that K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> possesses some extent of absorption at 532 nm. This is approximately half that of KABO powder (0.9 times of KDP) with the same particle size, which is in good agreement with the calculation results given above. The experiment and calculation show that the significant reduction of SHG coefficient of K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> with respect to KABO can be solely attributed to the larger twisting of the  $BO_3$  groups, while the absorption caused by  $Fe^{3+}$  ions contributes to a much lesser extent. It is worth mentioning that when the twisting angle goes towards 60°, all the contributions of the BO<sub>3</sub> groups to the SHG coefficients will be cancelled. Compared with KABO crystal, K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> has a lower congruent melting point at about 851 °C (see Appendices, Fig. A2) which makes it possible to be grown by the Czochralski method. In addition, another alkali metal borate Rb<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> has also been synthesized, which possesses similar XRD peaks (see Appendices, Fig. A3) but exhibits no SHG effects.

One of the other interesting aspects of the structure as mentioned above is that all the three  $Fe^{3+}$  ions sit in tetrahedrally coordinated environments. The lack of inversion symmetry relaxes the parity selection rule, thus leading to the emergence of some spin-forbidden bands dominating the transmittance spectrum of  $K_2Fe_2B_2O_7$  in the visible region (shown in Fig. 4). These bands can be ascribed to d-d transitions of tetrahedrally



**Fig. 1.** (a) Crystal structure of  $K_2Fe_2B_2O_7$  showing FeO<sub>4</sub> tetrahedral groups in blue and BO<sub>3</sub> trigonal groups in green (Fe, blue spheres; B, green spheres; K, black spheres; Oxygen atoms omitted for clarity). (b) Ball-and-stick representation of individual six-membered ring containing three BO<sub>3</sub> and three FeO<sub>4</sub> units and (c) the two different types of FeO<sub>4</sub> tetrahedral pairs. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

## Table 2

Selected inter-atomic distances (Å) and bond angles (°) for  $K_2Fe_2B_2O_7.$ 

K1-O2( × 2)	2.9901(7)	K2-01 <sup>i</sup>	3.0872(10)
K1–O3( × 2)	3.237(2)	K2-O3( × 2)	2.635(2)
K1-O4( × 2)	3.006(2)	K2-O4( × 2)	2.730(2)
K1-O5( × 2)	2.682(2)	K2-O5( × 2)	3.232(2)
In FeO <sub>4</sub> Tetrahedra			
Fe1-01	1.7917(8)	01-Fe1-05	108.66(7)
Fe1-05( × 3)	1.877(2)	05-Fe1-05	110.27(7)
Fe2–O2 <sup>ii</sup>	1.800(3)	04-Fe2-02 <sup>ii</sup>	107.69(7)
Fe2-O4( × 3)	1.868(2)	04-Fe2-04	111.19(7)
Fe3-02	1.799(3)	03-Fe3-02	108.15(7)
Fe3-03( × 3)	1.872(2)	03-Fe3-03	110.76(7)
In $BO_3$ Triangles			
B-O3 <sup>iii</sup>	1.379(4)	03 <sup>iii</sup> -B-04	118.8(3)
B-O4 <sup>iv</sup>	1.367(4)	04 <sup>iv</sup> -B-05 <sup>v</sup>	121.1(3)
B-O5 <sup>v</sup>	1.375(4)	03 <sup>iii</sup> -B-O5 <sup>v</sup>	120.1(3)

Symmetry codes: (i) x + 1, y, z, (ii) y, x, -z+2, (iii) -x+y, -x+1, z, (iv) x-1, y, z and (v) -y, x-y, z.

coordinated Fe<sup>3+</sup> ions,  ${}^{6}A_{1} \rightarrow {}^{4}T_{2}$  (<sup>4</sup>D) at 442 nm,  ${}^{6}A_{1} \rightarrow {}^{4}T_{2}$  (<sup>4</sup>G) at 510 nm and  ${}^{6}A_{1} \rightarrow {}^{4}T_{1}$  (<sup>4</sup>G) at 625 nm, respectively. These assignments are also in agreement with the *d*-*d* transitions of partially Fe<sup>3+</sup> doped KABO crystal [22]. Although the existence of Fe always results in absorptions in the UV and visible region, such Fe-containing materials (e.g. FeBO<sub>3</sub>, *R*Fe<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>, Fe(IO<sub>3</sub>)<sub>3</sub> [30]) are still widely studied for magnetic and NLO applications at longer wavelength in visible and infrared region. It is noteworthy that K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> is optically transparent from 500 to 2000 nm (Fig. 4) and this gives it practicability for potential optical applications in the future.

## 3.2. Magnetism

The temperature dependence of the magnetic susceptibilities of  $K_2Fe_2B_2O_7$  in both ZFC and FC conditions is shown in Fig. 5.

Above 30 K, K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> exhibits paramagnetic behavior. Unfortunately, in respect that the powder sample of the title compound is easy to decompose in atmosphere and only a small quantity (7 mg) of single crystals available for measurement relative to the assistant diamagnetic materials, the exact value of effective magnetic-moment ( $\mu_{eff}$ ) for each Fe<sup>3+</sup> ion cannot be obtained here. A susceptibility maximum in ZFC curve is observed at 20 K, which can be attributed as the evidence of spin-glass at the freezing temperature ( $T_f=20$  K), as the ZFC and FC susceptibility curves diverge at  $T_f$ . Magnetic ions embedded in borates can often form a triangular lattice with layered structures owing to the planar BO<sub>3</sub> triangular groups. Materials featuring such triangular lattices consisting of corner-sharing or edgesharing triangles are predicted to have no long range order in the lowest temperature due to competing AFM coupling between the nearest-neighbor spins [31-33]. In the past few years, several transition-metal borates have been found to show magnetic frustrations, such as LiMnBO<sub>3</sub> with a triangular magnetic lattice, YCa<sub>3</sub>(MnO)<sub>3</sub>(BO<sub>3</sub>)<sub>4</sub>, and Ca<sub>4</sub>(MnO)<sub>3</sub>(BO<sub>3</sub>)<sub>3</sub>CO<sub>3</sub> with a Kagomé lattice [34–36], particularly. The interaction between the linear Fe-O-Fe bonds connecting the triangular layer can be expected to be AFM through 180° superexchange and the Fe-O-B-O-Fe pathway in the triangular layer (with nearest Fe-Fe distance of 5.064 Å) is also possibly AFM. It is probably the latter in-plane AFM interaction, which gives rise to the spin frustration. Further magnetic structural studies (e.g. neutron diffraction) are necessary to reveal the actual magnetic interactions among the magnetic ions within the plane and among the layers.

#### 4. Conclusion

A new noncentrosymmetric ferroborate,  $K_2Fe_2B_2O_7$ , has been prepared as single crystal form and is found to crystallize in the trigonal space group *P*321. It possesses a layered structure composed of FeO<sub>4</sub> tetrahedra and BO<sub>3</sub> triangle groups forming a triangular Fe lattice in the *ab* plane.  $K_2Fe_2B_2O_7$  crystal is



Fig. 2. Arrangement of BO<sub>3</sub> triangles in K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> (a) and KABO (b) crystals viewed along the c axis.



Fig. 3. SHG intensity versus particle size for crushed K<sub>2</sub>Fe<sub>2</sub>B<sub>2</sub>O<sub>7</sub> crystal.



**Fig. 4.** Optical transmittance spectrum collected from  $K_2Fe_2B_2O_7$  crystal. Three absorption bands are ascribed to d-d transitions of tetrahedrally coordinated  $Fe^{3+}$  ions: 442 nm ( ${}^{6}A_1 \rightarrow {}^{4}T_2$  ( ${}^{4}D$ )), 520 nm ( ${}^{6}A_1 \rightarrow {}^{4}T_2$  ( ${}^{4}G$ )) and 630 nm ( ${}^{6}A_1 \rightarrow {}^{4}T_1$  ( ${}^{4}G$ )), respectively.

transparent in the 500–2000 nm region with three optical absorption bands attributed to d-d transitions of tetrahedrally coordinated Fe<sup>3+</sup> ions. Both the powder SHG test and the



**Fig. 5.** Temperature dependence of the magnetic susceptibilities (FC and ZFC) in the temperature range 5-400 K of  $K_2Fe_2B_2O_7$  under applied field of 1000 G, and their reciprocals (blue line) as a function of temperature (the inset shows the triangular Fe lattice in the *ab* plane). For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.

calculation show that its SHG efficiency is about 0.4 times that of KDP. Spin-glass behavior is observed below 20K which is attributed to geometrically magnetic frustration among Fe-ions in the triangular net.

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#### Appendix A. Supplementary material

Supplementary data associated with this article can be found in the online version at doi:10.1016/j.jssc.2010.03.037.

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